

Nicolò Dal Fabbro



Pushing the Boundaries of Federated Learning: Superlinear Convergence and Reinforcement Learning over Wireless

GTTI meeting September, 2024



Università degli Studi di Padova

Advisors: Prof. Luca Schenato Prof. Michele Rossi



Distributed Machine Learning



Massive data production

Artificial Intelligence = Data-Driven Algorithms

Distributed Machine Learning



Massive data production

Artificial Intelligence = Data-Driven Algorithms

Privacy

Decentralized datasets

Parallelization

Distributed Machine Learning



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Federated Learning

Federated Learning



Challenge: reducing the amount of communication

Federated Learning



In this thesis:

- Design communication efficient algorithms
- Analyze the effect of communication constraints on algorithms' convergence

1. Can we design **communication-efficient** algorithms for federated learning with **superlinear convergence**?

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1. Can we design **communication-efficient** algorithms for federated learning with **superlinear convergence**?

2. Can we provide finite-time analyses of **federated reinforcement learning** algorithms under **communication constraints**?

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2. Can we provide finite-time analyses of **federated reinforcement learning** algorithms under **communication constraints**?



Agent 1 Agent 2



Federated Learning

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Communication-efficient second-order methods

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SHED: an original algorithm based on Hessian eigenvectors sharing

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Theoretical foundations: the benefits of cooperation under communication constraints

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Luca Schenato Unipd



Michele Rossi Unipd



Subhrakanti Dey, Uppsala University

Superlinear federated learning: notation

M agents with datasets $\{\mathcal{D}_1, ..., \mathcal{D}_M\}$ aim to iteratively minimize a cost function $f(\boldsymbol{\theta}) = \frac{1}{M} \sum_{i=1}^{M} f_i(\boldsymbol{\theta})$

- $\theta^t \in \mathbb{R}^n$ is the *n*-dimensional global parameter at iteration *t*,
- $f_i(\theta)$ is the local cost of agent *i*,
- $U_t^{(i)}$ is the optimization set shared by agent *i* at iteration *t*.



Distributed gradient descent

Let $\mathbf{g}_t = \nabla f(\boldsymbol{\theta}^t) \in \mathbb{R}^n$ and $\mathbf{H}_t = \nabla^2 f(\boldsymbol{\theta}^t) \in \mathbb{R}^{n \times n}$ denote the gradient and the Hessian matrix of the cost function.

Distributed gradient descent consists of iteratively performing:

$$\boldsymbol{\theta}^{t+1} = \boldsymbol{\theta}^t - \eta_t \mathbf{g}_t$$

where η_t is the step size. We have assumed w.l.o.g. that all agents have the same number of data samples.

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$$\boldsymbol{\theta}^{t+1} = \boldsymbol{\theta}^t - \eta_t \mathbf{g}_t = \boldsymbol{\theta}^t - \eta_t (\frac{1}{M} \sum_{i=1}^M \mathbf{g}_t^{(i)}),$$

where η_t is the step size. We have assumed w.l.o.g. that all agents have the same number of data samples.

Pros: scales well

Cons: convergence rate heavily impacted by the condition number

Distributed Newton method

Let $\mathbf{g}_t = \nabla f(\boldsymbol{\theta}^t) \in \mathbb{R}^n$ and $\mathbf{H}_t = \nabla^2 f(\boldsymbol{\theta}^t) \in \mathbb{R}^{n \times n}$ denote the gradient and the Hessian matrix of the cost function.

The Newton method consists of iteratively performing the Newton update:

 $\boldsymbol{\theta}^{t+1} = \boldsymbol{\theta}^t - \eta_t \mathbf{H}_t^{-1} \mathbf{g}_t$

where η_t is the step size. We have assumed w.l.o.g. that all agents have the same number of data samples.

Distributed Newton method

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$$\boldsymbol{\theta}^{t+1} = \boldsymbol{\theta}^t - \eta_t \mathbf{H}_t^{-1} \mathbf{g}_t = \boldsymbol{\theta}^t - \eta_t (\frac{1}{M} \sum_{i=1}^M \mathbf{H}_t^{(i)})^{-1} (\frac{1}{M} \sum_{i=1}^M \mathbf{g}_t^{(i)}),$$

where η_t is the step size. We have assumed w.l.o.g. that all agents have the same number of data samples.

Pros: superlinear convergence speed independent of the condition number

Cons: significantly more demanding from a computation and communication point of view

$$\mathbf{g}_t^{(i)} = \nabla f_i(\boldsymbol{\theta}^t) \in \mathbb{R}^n$$





Approximate Newton method

Approximate Newton-type methods use approximations of the Hessian, \hat{H}_t , so a Newton-type parameter update is

$$\boldsymbol{\theta}^{t+1} = \boldsymbol{\theta}^t - \eta_t \hat{\boldsymbol{\mathsf{H}}}_t^{-1} \boldsymbol{\mathsf{g}}_t$$

where \hat{H}_t is an approximation of the Hessian matrix.

Question: can we provide superlinear convergence in a communication-efficient way?

N. Dal Fabbro, S. Dey, M. Rossi and L. Schenato, "SHED: A Newton-type algorithm for federated learning based on incremental Hessian eigenvector sharing", 2024, *Automatica*

N. Dal Fabbro, M. Rossi, L. Schenato, S. Dey "Q-SHED: Distributed Optimization at the Edge via Hessian Eigenvectors Quantization", *IEEE International Conference on Communications*, Rome 2023

State of the art

Wang, Shusen, et al. 'GIANT: Globally improved approximate newton method for distributed optimization.' *Advances in Neural Information Processing Systems* 31 (2018).

Rixon Crane and Fred Roosta. 'DINGO: Distributed Newton-type method for gradient-norm optimization'. *Advances in Neural Information Processing Systems* 32 (2019).

Safaryan, Mher, et al. 'FedNL: Making Newton-type methods applicable to federated learning.' *International Conference on Machine Learning* 39 (2022).

Agafonov, Artem, et al. 'FLECS: A Federated Learning Second-Order Framework via Compression and Sketching.' arXiv preprint arXiv:2206.02009 (2022)

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SHED: a Newton-type algorithm for FL based on eigendecomposition



Strengths of SHED

- Global convergence with asymptotic superlinear rate
- Versatility each agent can share a number of eigenvectors based on their communication resources
- Only **sporadic** Hessian computations required





This thesis

Federated Learning

Communication-efficient second-order methods

SHED: an original algorithm based on Hessian eigenvectors sharing

Federated reinforcement learning

Theoretical foundations: the benefits of cooperation under communication constraints

Aritra Mitra NCState

George Pappas Upenn

Arman Adibi Princeton

Vince Poor Princeton

Hamed Hassani Upenn Sanjeev Kulkarni Princeton

Federated reinforcement learning

Is it possible to provide finite-sample analysis for federated reinforcement learning under communication constraints?

• Goal

- Finite-sample convergence guarantees
- Achieve a linear convergence speedup w.r.t. the number of agents N
- Challenges
 - Markovian sampling
 - Communication constraints
 - (e.g., wireless networks)

Federated Learning

Distributed optimization under communication constraints

Li, T., Sahu, A. K., Talwalkar, A., and Smith, V. (2020). Federated learning: Challenges, methods, and future directions. *IEEE signal processing magazine*, *37*(3), 50-60.

Amiri, Mohammad Mohammadi, and Deniz Gündüz. "Federated learning over wireless fading channels." *IEEE Transactions on Wireless Communications* 19.5 (2020): 3546-3557.

Konečný, Jakub, et al. "Federated learning: Strategies for improving communication efficiency." *arXiv preprint arXiv:1610.05492* (2016).

Chen, Mingzhe, et al. "A joint learning and communications framework for federated learning over wireless networks." *IEEE Transactions on Wireless Communications* (2020)

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Federated Reinforcement Learning

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Federated Reinforcement Learning

Contributions

We provide the first finite-sample convergence analysis for federated reinforcement learning under communication constraints, establishing a linear convergence speedup with the number of agents

Temporal difference (TD) learning

 $\boldsymbol{\theta}_{k+1} = \boldsymbol{\theta}_k + \alpha \mathbf{g}_k(\boldsymbol{\theta}_k, o_k)$

Finite-sample analysis of this update rule under Markovian sampling has been recently established and provides

Bhandari, Jalaj, Daniel Russo, and Raghav Singal. "A finite time analysis of temporal difference learning with linear function approximation." *Conference on learning theory*, 2018

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 approximation error after T iterations

In federated RL with $\,N\,$ agents, can we obtain

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Federated TD learning

 $\mathbf{g}_{i,k}(\boldsymbol{\theta}_k, o_{i,k})$

TD update direction of agent i at iteration k

$$o_{i,k} = (s_{i,k}, r_{i,k}, s_{i,k+1})$$

Observation of agent i at iteration k

Federated TD learning over quantized communication: QFedTD

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N. Dal Fabbro, A. Mitra, G. J. Pappas, "Federated TD Learning over Finite-Rate Erasure Channels: Linear Speedup under Markovian Sampling". IEEE Control Systems Letters, 2023 47

Over-the-air federated TD learning: OAC-FedTD

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TD update direction of agent i at iteration k

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Observation of agent i at iteration k

$$\boldsymbol{\theta}_{k+1} = \boldsymbol{\theta}_k + \alpha \mathbf{v}_k$$
 $\mathbf{v}_k = \frac{1}{N} \sum_{i=1}^N h_{i,k} \mathbf{g}_{i,k}(\boldsymbol{\theta}_k, o_{i,k}) + \mathbf{w}_k$

N. Dal Fabbro, A. Mitra, R. W. Heath, L. Schenato, G. J. Pappas, "Over-the-Air Federated TD Learning" MLSys 2023 Workshop on Resource-Constrained Learning in Wireless Networks, Miami, Florida, 2023

Over-the-air federated TD learning: OAC-FedTD

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Asynchronous multi-agent TD learning: AsyncMATD

Finite-Time Analysis of Asynchronous Multi-Agent TD Learning

Main Result

Theorem (convergence analysis of QFedTD)

If $\alpha > 0$ small enough, then the iterates of QFedTD are such that

$$\mathbb{E}\left[\|\boldsymbol{\theta}^* - \boldsymbol{\theta}_T\|^2\right] \leq \underbrace{C_1(1 - \alpha p C_0)^T}_{\text{bias term}} + \underbrace{O\left(\frac{\zeta \alpha \tau \sigma^2}{N}\right)}_{\text{statistical terms}} + \underbrace{\bigcup}_{\text{negligible terms}}$$

Main takeaways: we show the impact of the **channel effects** ζ and p on the convergence. We establish a linear convergence speedup with the number of agents N. We obtain a linear dependence on the mixing time of the Markov chain, τ .

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Theoretical foundations: the benefits of cooperation under communication constraints

Future directions

Superlinear FL:

• Scaling up existing algorithms from a computational point of view

FRL:

 Heterogeneity/personalization, local optimization
 Federated Multi-Agent reinforcement learning sample complexity and communications even more critical

PhD thesis publications

Journals

N. Dal Fabbro, S. Dey, M. Rossi and L. Schenato, "SHED: A Newton-type algorithm for federated learning based on incremental Hessian eigenvector sharing", *Automatica*, 2024

N. Dal Fabbro, A. Mitra, G. J. Pappas, "Federated TD Learning over Finite-Rate Erasure Channels: Linear Speedup under Markovian Sampling". *IEEE Control Systems Letters*, 2023

Conferences

N. Dal Fabbro, M. Rossi, L. Schenato, S. Dey "Q-SHED: Distributed Optimization at the Edge via Hessian Eigenvectors Quantization", *IEEE International Conference on Communications*, Rome 2023

N. Dal Fabbro, A. Mitra, R. W. Heath, L. Schenato, G. J. Pappas, "Over-the-Air Federated TD Learning" *MLSys 2023* Workshop on Resource-Constrained Learning in Wireless Networks, Miami, Florida, 2023

A.Adibi, **N. Dal Fabbro**, L. Schenato, S. Kulkarni, H. V. Poor, G. J. Pappas, H. Hassani and A. Mitra. Stochastic Approximation with Delayed Updates: Finite-Time Rates under Markovian Sampling, *AISTATS*, 2024

N. Dal Fabbro, Arman Adibi, Aritra Mitra, George J. Pappas. Finite-Time Analysis of Asynchronous Multi-Agent TD Learning, *The 2024 American Control Conference (ACC)*, 2024

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Advisors: Prof. Luca Schenato Prof. Michele Rossi Thank you!